# Quiz-II, SBDA131C 

Date: 21-11-17
Maximum Marks-20
Time: 40 Mins.

1. A study is conducted concerning the blood pressure of 60 year old women with glaucoma. In the study 200 sixty-year old women with glaucoma are randomly selected and the sample mean systolic blood pressure is 140 mm Hg and the sample standard deviation is 25 mm Hg .
a. Calculate a $95 \%$ confidence interval for the true mean systolic blood pressure among the population of 60 year old women with glaucoma.
b. Suppose the study above was based on 100 women instead of 200 but the sample mean (140) and standard deviation (25) are the same. Recalculate the $95 \%$ confidence interval. Does the interval get wider or narrower? Why?
c. Calculate the $99 \%$ confidence interval (CI) for the mean systolic blood pressure. Why the $99 \%$ CI is wider or narrower than $95 \%$ ? Give reasons for your answer.
2. Nakamura et al. studied subjects with medial collateral ligament (MCL) and anterior cruciate ligament (ACL) tears. Between February 1995 and December 1997, 17 consecutive patients with combined acute ACL and grade III MCL injuries were treated by the same physician at the research center. One of the variables of interest was the length of time in days between the occurrence of the injury and the first magnetic resonance imaging (MRI). The data are shown in Table below. Can you conclude that the mean number of days between injury and initial MRI is not 15 days in a population presumed to be represented by these sample data. Justify your answer by performing 10 step Hypothesis test.

| Subject: | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Days: | 14 | 9 | 18 | 26 | 12 | 0 | 10 | 4 | 8 | 21 | 28 | 24 | 2 | 2 | 3 | 14 | 9 |

Find out a $95 \%$ confidence interval and compare it with your conclusion drawn through hypothesis test.

STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

| Z | . 00 | . 01 | . 02 | . 03 | . 04 | . 05 | . 06 | . 07 | . 08 | . 09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3.9 | . 00005 | . 00005 | . 00004 | . 00004 | . 00004 | . 00004 | . 00004 | . 00004 | . 00003 | . 00003 |
| -3.8 | . 00007 | . 00007 | . 00007 | . 00006 | . 00006 | . 00006 | . 00006 | . 00005 | . 00005 | . 00005 |
| -3.7 | . 00011 | . 00010 | . 00010 | . 00010 | . 00009 | . 00009 | . 00008 | . 00008 | . 00008 | . 00008 |
| -3.6 | . 00016 | . 00015 | . 00015 | . 00014 | . 00014 | . 00013 | . 00013 | . 00012 | . 00012 | . 00011 |
| -3.5 | . 00023 | . 00022 | . 00022 | . 00021 | . 00020 | . 00019 | . 00019 | . 00018 | . 00017 | . 00017 |
| -3.4 | . 00034 | . 00032 | . 00031 | . 00030 | . 00029 | . 00028 | . 00027 | . 00026 | . 00025 | . 00024 |
| -3.3 | . 00048 | . 00047 | . 00045 | . 00043 | . 00042 | . 00040 | . 00039 | . 00038 | . 00036 | . 00035 |
| -3.2 | . 00069 | . 00066 | . 00064 | . 00062 | . 00060 | . 00058 | . 00056 | . 00054 | . 00052 | . 00050 |
| -3.1 | . 00097 | . 00094 | . 00090 | . 00087 | . 00084 | . 00082 | . 00079 | . 00076 | . 00074 | . 00071 |
| -3.0 | . 00135 | . 00131 | . 00126 | . 00122 | . 00118 | . 00114 | . 00111 | . 00107 | . 00104 | . 00100 |
| -2.9 | . 00187 | . 00181 | . 00175 | . 00169 | . 00164 | . 00159 | . 00154 | . 00149 | . 00144 | . 00139 |
| -2.8 | . 00256 | . 00248 | . 00240 | . 00233 | . 00226 | . 00219 | . 00212 | . 00205 | . 00199 | . 00193 |
| -2.7 | . 00347 | . 00336 | . 00326 | . 00317 | . 00307 | . 00298 | . 00289 | . 00280 | . 00272 | . 00264 |
| -2.6 | . 00466 | . 00453 | . 00440 | . 00427 | . 00415 | . 00402 | . 00391 | . 00379 | . 00368 | . 00357 |
| -2.5 | . 00621 | . 00604 | . 00587 | . 00570 | . 00554 | . 00539 | . 00523 | . 00508 | . 00494 | . 00480 |
| -2.4 | . 00820 | . 00798 | . 00776 | . 00755 | . 00734 | . 00714 | . 00695 | . 00676 | . 00657 | . 00639 |
| -2.3 | . 01072 | . 01044 | . 01017 | . 00990 | . 00964 | . 00939 | . 00914 | . 00889 | . 00866 | . 00842 |
| -2.2 | . 01390 | . 01355 | . 01321 | . 01287 | . 01255 | . 01222 | . 01191 | . 01160 | . 01130 | . 01101 |
| -2.1 | . 01786 | . 01743 | . 01700 | . 01659 | . 01618 | . 01578 | . 01539 | . 01500 | . 01463 | . 01426 |
| -2.0 | . 02275 | . 02222 | . 02169 | . 02118 | . 02068 | . 02018 | . 01970 | . 01923 | . 01876 | . 01831 |
| -1.9 | . 02872 | . 02807 | . 02743 | . 02680 | . 02619 | . 02559 | . 02500 | . 02442 | . 02385 | . 02330 |
| -1.8 | . 03593 | . 03515 | . 03438 | . 03362 | . 03288 | . 03216 | . 03144 | . 03074 | . 03005 | . 02938 |
| -1.7 | . 04457 | . 04363 | . 04272 | . 04182 | . 04093 | . 04006 | . 03920 | . 03836 | . 03754 | . 03673 |
| -1.6 | . 05480 | . 05370 | . 05262 | . 05155 | . 05050 | . 04947 | . 04846 | . 04746 | . 04648 | . 04551 |
| -1.5 | . 06681 | . 06552 | . 06426 | . 06301 | . 06178 | . 06057 | . 05938 | . 05821 | . 05705 | . 05592 |
| -1.4 | . 08076 | . 07927 | . 07780 | . 07636 | . 07493 | . 07353 | . 07215 | . 07078 | . 06944 | . 06811 |
| -1.3 | . 09680 | . 09510 | . 09342 | . 09176 | . 09012 | . 08851 | . 08691 | . 08534 | . 08379 | . 08226 |
| -1.2 | . 11507 | . 11314 | . 11123 | . 10935 | . 10749 | . 10565 | . 10383 | . 10204 | . 10027 | . 09853 |
| -1.1 | . 13567 | . 13350 | . 13136 | . 12924 | . 12714 | . 12507 | . 12302 | . 12100 | . 11900 | . 11702 |
| -1.0 | . 15866 | . 15625 | . 15386 | . 15151 | . 14917 | . 14686 | . 14457 | . 14231 | . 14007 | . 13786 |
| -0.9 | . 18406 | . 18141 | . 17879 | . 17619 | . 17361 | . 17106 | . 16853 | . 16602 | . 16354 | . 16109 |
| -0.8 | . 21186 | . 20897 | . 20611 | . 20327 | . 20045 | . 19766 | . 19489 | . 19215 | . 18943 | . 18673 |
| -0.7 | . 24196 | . 23885 | . 23576 | . 23270 | . 22965 | . 22663 | . 22363 | . 22065 | . 21770 | . 21476 |
| -0.6 | . 27425 | . 27093 | . 26763 | . 26435 | . 26109 | . 25785 | . 25463 | . 25143 | . 24825 | . 24510 |
| -0.5 | . 30854 | . 30503 | . 30153 | . 29806 | . 29460 | . 29116 | . 28774 | . 28434 | . 28096 | . 27760 |
| -0.4 | . 34458 | . 34090 | . 33724 | . 33360 | . 32997 | . 32636 | . 32276 | . 31918 | . 31561 | . 31207 |
| -0.3 | . 38209 | . 37828 | . 37448 | . 37070 | . 36693 | . 36317 | . 35942 | . 35569 | . 35197 | . 34827 |
| -0.2 | . 42074 | . 41683 | . 41294 | . 40905 | . 40517 | . 40129 | . 39743 | . 39358 | . 38974 | . 38591 |
| -0.1 | . 46017 | . 45620 | . 45224 | . 44828 | . 44433 | . 44038 | . 43644 | . 43251 | . 42858 | . 42465 |
| -0.0 | . 50000 | . 49601 | . 49202 | . 48803 | . 48405 | . 48006 | . 47608 | . 47210 | . 46812 | . 46414 |

F - Distribution ( $\alpha=0.05$ in the Right Tail)

|  | Numerator Degrees of Freedom |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 241.88 | 243.91 | 245.95 | 248.01 | 249.05 | 250.10 | 251.14 | 252.20 | 253.25 | 254.31 |
| 2 | 19.396 | 19.413 | 19.429 | 19.446 | 19.454 | 19.462 | 19.471 | 19.479 | 19.487 | 19.496 |
| 3 | 8.7855 | 8.7446 | 8.7029 | 8.6602 | 8.6385 | 8.6166 | 8.5944 | 8.5720 | 8.5494 | 8.5264 |
| 4 | 5.9644 | 5.9117 | 5.8578 | 5.8025 | 5.7744 | 5.7459 | 5.7170 | 5.6877 | 5.6581 | 5.6281 |
| 5 | 4.7351 | 4.6777 | 4.6188 | 4.5581 | 4.5272 | 4.4957 | 4.4638 | 4.4314 | 4.3985 | 4.3650 |
| 6 | 4.0600 | 3.9999 | 3.9381 | 3.8742 | 3.8415 | 3.8082 | 3.7743 | 3.7398 | 3.7047 | 3.6689 |
| 7 | 3.6365 | 3.5747 | 3.5107 | 3.4445 | 3.4105 | 3.3758 | 3.3404 | 3.3043 | 3.2674 | 3.2298 |
| 8 | 3.3472 | 3.2839 | 3.2184 | 3.1503 | 3.1152 | 3.0794 | 3.0428 | 3.0053 | 2.9669 | 2.9276 |
| - 9 | 3.1373 | 3.0729 | 3.0061 | 2.9365 | 2.9005 | 2.8637 | 2.8259 | 2.7872 | 2.7475 | 2.7067 |
| E 10 | 2.9782 | 2.9130 | 2.8450 | 2.7740 | 2.7372 | 2.6996 | 2.6609 | 2.6211 | 2.5801 | 2.5379 |
| -8 11 | 2.8536 | 2.7876 | 2.7186 | 2.6464 | 2.6090 | 2.5705 | 2.5309 | 2.4901 | 2.4480 | 2.4045 |
| ${ }^{9} 12$ | 2.7534 | 2.6866 | 2.6169 | 2.5436 | 2.5055 | 2.4663 | 2.4259 | 2.3842 | 2.3410 | 2.2962 |
| 는 13 | 2.6710 | 2.6037 | 2.5331 | 2.4589 | 2.4202 | 2.3803 | 2.3392 | 2.2966 | 2.2524 | 2.2064 |
| \% 14 | 2.6022 | 2.5342 | 2.4630 | 2.3879 | 2.3487 | 2.3082 | 2.2664 | 2.2229 | 2.1778 | 2.1307 |
| ¢) 15 | 2.5437 | 2.4753 | 2.4034 | 2.3275 | 2.2878 | 2.2468 | 2.2043 | 2.1601 | 2.1141 | 2.0658 |
| - 16 | 2.4935 | 2.4247 | 2.3522 | 2.2756 | 2.2354 | 2.1938 | 2.1507 | 2.1058 | 2.0589 | 2.0096 |
| ¢ 17 | 2.4499 | 2.3807 | 2.3077 | 2.2304 | 2.1898 | 2.1477 | 2.1040 | 2.0584 | 2.0107 | 1.9604 |
| -18 | 2.4117 | 2.3421 | 2.2686 | 2.1906 | 2.1497 | 2.1071 | 2.0629 | 2.0166 | 1.9681 | 1.9168 |
| $\bigcirc 19$ | 2.3779 | 2.3080 | 2.2341 | 2.1555 | 2.1141 | 2.0712 | 2.0264 | 1.9795 | 1.9302 | 1.8780 |
| $\frac{0}{0} 20$ | 2.3479 | 2.2776 | 2.2033 | 2.1242 | 2.0825 | 2.0391 | 1.9938 | 1.9464 | 1.8963 | 1.8432 |
| .듣 21 | 2.3210 | 2.2504 | 2.1757 | 2.0960 | 2.0540 | 2.0102 | 1.9645 | 1.9165 | 1.8657 | 1.8117 |
| E 22 | 2.2967 | 2.2258 | 2.1508 | 2.0707 | 2.0283 | 1.9842 | 1.9380 | 1.8894 | 1.8380 | 1.7831 |
| - 23 | 2.2747 | 2.2036 | 2.1282 | 2.0476 | 2.0050 | 1.9605 | 1.9139 | 1.8648 | $1.8128$ | $1.7570$ |
| - 24 | 2.2547 | 2.1834 | 2.1077 | 2.0267 | 1.9838 | 1.9390 | 1.8920 | 1.8424 | 1.7896 | 1.7330 |
| 25 | 2.2365 | 2.1649 | 2.0889 | 2.0075 | 1.9643 | 1.9192 | 1.8718 | 1.8217 | 1.7684 | 1.7110 |
| 26 | 2.2197 | 2.1479 | 2.0716 | 1.9898 | 1.9464 | 1.9010 | 1.8533 | 1.8027 | 1.7488 | 1.6906 |
| 27 | 2.2043 | 2.1323 | 2.0558 | 1.9736 | 1.9299 | 1.8842 | 1.8361 | 1.7851 | 1.7306 | 1.6717 |
| 28 | 2.1900 | 2.1179 | 2.0411 | 1.9586 | 1.9147 | 1.8687 | 1.8203 | 1.7689 | 1.7138 | 1.6541 |
| 29 | 2.1768 | 2.1045 | 2.0275 | 1.9446 | 1.9005 | 1.8543 | 1.8055 | 1.7537 | 1.6981 | 1.6376 |
| 30 | 2.1646 | 2.0921 | 2.0148 | 1.9317 | 1.8874 | 1.8409 | 1.7918 | 1.7396 | 1.6835 | 1.6223 |
| 40 | 2.0772 | 2.0035 | 1.9245 | 1.8389 | 1.7929 | 1.7444 | 1.6928 | 1.6373 | 1.5766 | 1.5089 |
| 60 | 1.9926 | 1.9174 | 1.8364 | 1.7480 | 1.7001 | 1.6491 | 1.5943 | 1.5343 | 1.4673 | 1.3893 |
| 120 | 1.9105 | 1.8337 | 1.7505 | 1.6587 | 1.6084 | 1.5543 | 1.4952 | 1.4290 | 1.3519 | 1.2539 |
| $\infty$ | 1.8307 | 1.7522 | 1.6664 | 1.5705 | 1.5173 | 1.4591 | 1.3940 | 1.3180 | 1.2214 | 1.0000 |


| cum. prob | $t_{\text {. } 50}$ | $t_{\text {t }} 7$ | $t_{.80}$ | $t_{\text {. }}{ }^{\text {b }}$ | $t_{\text {. }}^{\text {g }}$ | $t_{\text {t }} 9$ | ${ }_{\text {t }}^{975}$ | $t_{\text {t } 99}$ | $t_{\text {t }}^{\text {g }}$ ( | $t_{\text {t }}^{\text {g }}$ 99 | $t_{\text {. } 9995}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| one-tail | 0.50 | 0.25 | 0.20 | 0.15 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 | 0.001 | 0.0005 |
| two-tails | 1.00 | 0.50 | 0.40 | 0.30 | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 | 0.002 | 0.001 |
| df |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 0.000 | 1.000 | 1.376 | 1.963 | 3.078 | 6.314 | 12.71 | 31.82 | 63.66 | 318.31 | 636.62 |
| 2 | 0.000 | 0.816 | 1.061 | 1.386 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 22.327 | 31.599 |
| 3 | 0.000 | 0.765 | 0.978 | 1.250 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 10.215 | 12.924 |
| 4 | 0.000 | 0.741 | 0.941 | 1.190 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 7.173 | 8.610 |
| 5 | 0.000 | 0.727 | 0.920 | 1.156 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5.893 | 6.869 |
| 6 | 0.000 | 0.718 | 0.906 | 1.134 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 5.208 | 5.959 |
| 7 | 0.000 | 0.711 | 0.896 | 1.119 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 4.785 | 5.408 |
| 8 | 0.000 | 0.706 | 0.889 | 1.108 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 4.501 | 5.041 |
| 9 | 0.000 | 0.703 | 0.883 | 1.100 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 4.297 | 4.781 |
| 10 | 0.000 | 0.700 | 0.879 | 1.093 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 4.144 | 4.587 |
| 11 | 0.000 | 0.697 | 0.876 | 1.088 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 4.025 | 4.437 |
| 12 | 0.000 | 0.695 | 0.873 | 1.083 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 3.930 | 4.318 |
| 13 | 0.000 | 0.694 | 0.870 | 1.079 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 3.852 | 4.221 |
| 14 | 0.000 | 0.692 | 0.868 | 1.076 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 3.787 | 4.140 |
| 15 | 0.000 | 0.691 | 0.866 | 1.074 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 3.733 | 4.073 |
| 16 | 0.000 | 0.690 | 0.865 | 1.071 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 3.686 | 4.015 |
| 17 | 0.000 | 0.689 | 0.863 | 1.069 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 3.646 | 3.965 |
| 18 | 0.000 | 0.688 | 0.862 | 1.067 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 3.610 | 3.922 |
| 19 | 0.000 | 0.688 | 0.861 | 1.066 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 3.579 | 3.883 |
| 20 | 0.000 | 0.687 | 0.860 | 1.064 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 3.552 | 3.850 |
| 21 | 0.000 | 0.686 | 0.859 | 1.063 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 3.527 | 3.819 |
| 22 | 0.000 | 0.686 | 0.858 | 1.061 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 3.505 | 3.792 |
| 23 | 0.000 | 0.685 | 0.858 | 1.060 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 3.485 | 3.768 |
| 24 | 0.000 | 0.685 | 0.857 | 1.059 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 3.467 | 3.745 |
| 25 | 0.000 | 0.684 | 0.856 | 1.058 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 3.450 | 3.725 |
| 26 | 0.000 | 0.684 | 0.856 | 1.058 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 3.435 | 3.707 |
| 27 | 0.000 | 0.684 | 0.855 | 1.057 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 3.421 | 3.690 |
| 28 | 0.000 | 0.683 | 0.855 | 1.056 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 3.408 | 3.674 |
| 29 | 0.000 | 0.683 | 0.854 | 1.055 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 3.396 | 3.659 |
| 30 | 0.000 | 0.683 | 0.854 | 1.055 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 3.385 | 3.646 |
| 40 | 0.000 | 0.681 | 0.851 | 1.050 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 | 3.307 | 3.551 |
| 60 | 0.000 | 0.679 | 0.848 | 1.045 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 | 3.232 | 3.460 |
| 80 | 0.000 | 0.678 | 0.846 | 1.043 | 1.292 | 1.664 | 1.990 | 2.374 | 2.639 | 3.195 | 3.416 |
| 100 | 0.000 | 0.677 | 0.845 | 1.042 | 1.290 | 1.660 | 1.984 | 2.364 | 2.626 | 3.174 | 3.390 |
| 1000 | 0.000 | 0.675 | 0.842 | 1.037 | 1.282 | 1.646 | 1.962 | 2.330 | 2.581 | 3.098 | 3.300 |
| z | 0.000 | 0.674 | 0.842 | 1.036 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | 3.090 | 3.291 |
|  | 0\% | 50\% | 60\% | 70\% | 80\% | 90\% | 95\% | 98\% | 99\% | 99.8\% | 99.9\% |
|  | Confidence Level |  |  |  |  |  |  |  |  |  |  |

